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Electrical and Computer Engineering

**CLASSIFICATION ON BREAST CANCER USING
GENETIC ALGORITHM TRAINED NEURAL
NETWORK**

Hiba Badri Hasan

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Asst. Prof. Dr. Sefer Kurnaz

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CLASSIFICATION ON BREAST CANCER USING GENETIC ALGORITHM TRAINED NEURAL NETWORK

by

Hiba Badri Hasan

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DEDICATION

I give my best efforts to my dear father and to my dear mother who have done everything they can for supporting me, and also thanks and appreciation to all those who stood with me and supported me in my studies.



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ABSTRACT

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Hasan, Hiba Badri

M.Sc., Electrical and Computer Engineering, Altınbaş University,

Supervisor: Asst Prof. Dr. Sefer kurnaz

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Artificial neural networks have been in the position of producing complex dynamics in control applications over the last decade, especially when they are linked to feedback. Although ANNs are strong for network design, the harder the design of the network, the more complex the desired dynamic is. Many researchers tried to automate the design process of ANN using computer programs. Search and optimization problems can be considered as the problem of finding the best parameter set for a network to solve a problem. Recently, the problem of optimizing ANN parameters to train different research datasets has been targeted by two commonly used stochastic genetic algorithms (GA). The process based on the neural network is optimized with GA to enable the robot to perform complex tasks. However, using such optimization algorithms to optimize the ANN training process cannot always be balanced or successful. These algorithms simultaneously aim to develop three main components of an ANN: synaptic weight, connections, architecture and transfer functions set for each neuron. Developed with the proposed approach, ANN is also compared with hand-designed Levenberg-Marquardt and Back Propagation algorithms.

Keywords: Artificial neural network, Backpropagation, Partial swarm optimization, Mean square error, optimization, classification.

ÖZET

GENETİK ALGORİTMA İLE EĞİTİMLİ YAPAY SİNİR AĞI KULLANILAN MEME KANSERİNİN SINIFLANDIRILMASI

Hasan, Hiba Badri

M.Sc., Electrical and Computer Engineering, Altınbaş University,

Danışman: Asst Prof. Dr. Sefer kurnaz

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Yapay sinir ağları, son on yılda kontrol uygulamalarında karmaşık dinamikleri üretme konumunda, özellikle de geri bildirime bağlı olduklarında olmuştur. YSA'lar ağ tasarımı için güçlü olsa da, ağın tasarımı ne kadar zorsa, istenen dinamik o kadar karmaşıktır. Birçok araştırmacı, bilgisayar programları kullanarak YSA'nın tasarım sürecini otomatikleştirmeye çalıştı. Arama ve optimizasyon problemleri, bir problemi çözmek için bir ağ için ayarlanmış en iyi parametreyi bulma problemi olarak düşünülebilir. Son zamanlarda, farklı araştırma veri kümelerini eğitmek için ANN parametrelerini optimize etme sorunu, yaygın olarak kullanılan iki stokastik genetik algoritma (GA) ile hedeflenmiştir. Sinir ağına dayanan süreç, robotun karmaşık görevleri yapmasını sağlamak için GA ile optimize edilmiştir. Bununla birlikte, YSA eğitim sürecini optimize etmek için bu tür optimizasyon algoritmalarını kullanmak her zaman dengeli veya başarılı olamaz. Bu algoritmalar aynı anda bir YSA'nın üç ana bileşenini geliştirmeyi amaçlar: her bir nöron için ayarlanmış sinaptik ağırlık, bağlantılar, mimari ve aktarım işlevleri. Önerilen yaklaşımla geliştirilen YSA, el tasarımı Levenberg-Marquardt ve Sirt Yayılım algoritmalarıyla da karşılaştırılmıştır.

Anahtar kelimeler: Yapay sinir ağı, Backpropagation, genetik Algoritma, Ortalama kare hatası, optimizasyon, sınıflandırma.

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1. INTRODUCTION

The neural system is arranged into hidden layers, input and output of the Artificial Neural Networks (ANNs). The neurons are joined together by a series of synaptic weights. An ANN is a powerful tool for identifying patterns, predictions and regressions in a variety of problems. The ANN continually changes its synaptic values during the learning process until sufficient acquired knowledge (until a certain number of iterations have been achieved or the error value of the target has been achieved). After completion of the learning or training stage, the ability of the ANN to generalize the problem with samples other than those employed during the training stage must be assessed. Finally, during training and testing, it is expected that the ANN will be able to accurately classify the patterns of a particular problem. In recent years several classic ANN algorithms have been suggested and developed. However, many of them can stay trapped in nondesirable solutions; that is, they will be far from the optimum or the best solution. Moreover, most of these algorithms cannot explore multimodal and noncontinuous surfaces.

Therefore, other kinds of techniques, such as bioinspired algorithms (BIAs), are necessary for training an ANN. As BIAs are strong optimization tools and can resolve very complicated optimization problems, they are well accepted by the Artificial Intelligence Community. For a given problem, BIAs can browse large multimodal and continuous search areas and find the optimum value for the best solution. BIAs is based on nature's behavior described as swarm intelligence. The term [1] defines this concept as being owned by unintelligent agents with limited individual capacities, but intelligent collective behavior.

There are several studies which use evolutionary and bio - inspired algorithms as a basic way of training ANN [2]. Metaheuristic methods for training neural networks are based on local search, population methods, and others such as cooperative coevolutionary models [3]. An excellent work in which the authors show a comprehensive literature review of evolving ANN algorithms [2]. The majority of the research reports however focus on the development of synaptic weight, parameters [4] or the evolution of the numbers of the neurons for hidden layers, but the designer determines the number of hidden layers previously. Moreover, the researchers do not involve the evolution of transfer functions, which are an important element of an ANN that determines the output of each neuron. In [5], for instance, the authors suggested a combining of the Ant Colony

Optimization (ACO) methodology to identify ANN and PSO for weight adjustment. Additional studies such as the [6] modify the Simulated Annealing (SA) PSO for the acquisition of a set of synaptic weight and threshold ANNs. In [7], the authors use Evolutionary Programming to obtain the architecture and weight to solve problems of classification and forecasting. Another example is [8] where Genetic Programming is used to obtain graphs that represent different topologies. In [9], the Differential Evolution (DE) algorithm was applied to design an ANN to solve a weather forecasting problem. In [10], the authors use a PSO algorithm to modify the synaptic weights to model the relationship between daily rains and runoffs in Malaya. In [11], the authors compare the back-propagation method versus basic PSO to adjust only the synaptic weights of an ANN for solving classification problems. In [12], the set of weights are evolved using the Differential Evolution and basic PSO. The three principal elements of an ANN were simultaneously developed in other works such as [13]: architecture, transfers and synaptic weights. In [14] the authors solved the same problem with a differential Evolution (DE) algorithm and suggested a new model with a PSO (NMPSO) algorithm for the authors. The author has also used [15] to develop the design of an ANN with two different fitness functions by using an Artificial Bee Colony (ABC) algorithm.

Therefore in this research work, we proposed a technique that uses PSO for ANN training to improve the training and testing performance of existing ANN on the diabetes dataset.

The chapters in this study focus are:

1. Chapter 1: The first chapter focuses on this thesis, which explains the idea and the purpose of this thesis. That makes a complete review of how this work can be done.
2. Chapter 2: The second chapter is the literature review of references to this thesis. Their results and the algorithms used to classify the dataset by other researchers are thoroughly reviewed.
3. Chapter 3: The third chapter focuses on the methodology for this thesis where the collection of data and the general look of ANN, GA and BP are explained. In addition, review a clear understanding of the characteristics of these algorithms and the ways they can be developed. It also gives a full idea of how GA and BP train an ANN and how these algorithms are being developed during their training. The advantages and disadvantages for ANN training are also presented by both BP and GA.

4. Chapter 4: This chapter provides a clear picture of the results of this study, which shows both GA and BP performance in ANN training and compares the results.
5. Chapter 5: The last chapter is the results and the recommendation that gives an overview of the results and summarizes the results from our experiments.

1.1 PURPOSE AND THESIS IMPORTANCE

This research aims to present a new optimization algorithm called GA, which will improve ANN's training performance. The fitness functions take into consideration the classification error, mean square error, validation error, architectural reduction or a combination. This research also explores the behaviours, using different parameter values, of three bioinspired algorithms. The best parameter values for these algorithms are determined to achieve optimum results during the experimentation phase. In addition, a number of statistically valid experiments are generated for each selected classification problem using the best configuration. Furthermore, the results of the proposed methodology are discussed with regard to the connection number, the neuron numbers and the transfer functions selected for each ANN.

1.2 METAHEURISTIC ALGORITHMS

A metaheuristic method in computer science and mathematical optimisation is designed to identify, create or select heuristic (partially searched algorithms) that can provide a good and adequate solution to the optimisation problem, especially if the information is incomplete, or imperfect, or if the calculator is limited. For sampling metaheuristics, a number of solutions are excessive. Metaheuristics can make few assumptions about the problem of optimization, and can therefore be used in a number of problems.

Metaheuristics cannot ensure that some types of problems are found to offer a global optimal solution in comparison with optimizing algorithms and iterative methods. Many metaheuristics are used to optimize the stochastic to make the solution dependent upon the set of random variables. When combined, metaheuristics often find solutions with less computational effort by looking for a wide array of feasible solutions than optimization Algorithms. Therefore, they are useful

solutions to optimization problems. There have been published a number of books and papers on this topic.

The majority of the metaheuristic literature is experimental, describing empirical findings from experiments with computer algorithms. However, formal theoretical results, often regarding convergence and the possibility of finding the global optimum are also available. Many metaheuristic methods have been published with novelty and practical efficiency. Although there was high quality research in the field, many publications were of bad quality; vagueness, inadequate design, poor experiments and ignorance of previous literature are some of the shortcomings.

1.2.1 Genetic Algorithm (GA)

In the late 1960s, the concept of GA was first introduced to the evolutionary theory by Holland and its colleagues. In nature, unsuitable and weak species face extinction by natural selection compared to their environment. The strongest species have more opportunities for reproductive transmission of their genes into future generations; this process takes time and is gradual. The species with the right gene combination will be more dominant over the long term. At times, random changes in the genes may take place during this slow process of evolution. These unintended variations offer additional benefits through diversification to the natural selection process. New species evolve from old species, unsuccessful modifications, and natural combinations automatically eliminate in this never-ending challenge of survival. In GA terminology, an individual or chromosome solution vector is referred to. These chromosomes consist of discrete units known as genes. One or more chromosome elements are controlled in each gene. The initial Holland GA implementation had binary numbers as genes. The latest deployments provided more representation and encoding of genes. A chromosome is usually the only solution in the space of the solution. GA works with the population, a set of chromosomes. The population is usually randomly initialized. As the algorithm runs, people with a higher fitness are progressively found ; each candidate has a number of properties (genotype) that can be mutated and therefore better solutions are found.

2. LITERATURE REVIEW

The Artificial Neural Networks (ANNs) are the neural system organized into hidden layers, input and output. The neurons are joined by a set of synaptic weights. An ANN is a powerful tool used to identify models, predictions and regressions in a variety of problems. The ANN continually changes its synaptic values during the learning process until sufficient acquired knowledge (until a certain number of iterations have been achieved or the error value of the target has been achieved). After the training stage, the capacity of ANN to generalize the problem must be evaluated with samples different from those used during the training stage. The problem should be generalized.

Several classic algorithms to train an ANN have been proposed and developed in the last years. However, many of them can stay trapped in nondesirable solutions; that is, they will be far from the optimum or the best solution. Moreover, most of these algorithms cannot explore multimodal and noncontinuous surfaces. Therefore, other kinds of techniques, such as bioinspired algorithms (BIAs), are necessary for training an ANN.

As BIAs are powerful optimizing instruments and can solve very complex optimizing issues, they have a positive support by artificial intelligence. BIAs can explore large multimodal and non - constant search areas for the best solution near the optimal value for a specific problem. BIAs are based on the behavior of nature described as the swarm. In [1] this concept is defined as owned by smart and limited personal agents with smart collective behavior.

There are several works that use evolutionary and bioinspired algorithms to train ANN as another fundamental form of learning [2]. Metaheuristic methods for training neural networks are based on local search, population methods, and others such as cooperative coevolutionary models [3].

The authors show a comprehensive literature review of evolutionary algorithms used for the development of ANN [2]. Most of the research reports are, however, focused exclusively on the development of synaptic weights, parameters [4] or evolution of the numbers of neurons in hidden layers. The designer determines the number of hidden layers. Moreover, the researches do not involve the evolution of transfer functions, which are an important element of an ANN that determines the output of each neuron.

For example, in [6] the authors suggested a method combining ANN and Particle Swarm Optimization (PSO) for a specific architecture (connections) to adjust the weight of the synaptical. Other research, such as [6], has carried out a modified PSO mixture with Simulated Annealing to obtain a set of ANN and ANN weights. [7] In order to find out the architecture and weights, authors use evolutionary programming to solve classification problems and forecasting problems. Another example is [8] where Genetic Programming is used to obtain graphs that represent different topologies. In [9], the Differential Evolution (DE) algorithm was applied to design an ANN to solve a weather forecasting problem. In [10], the authors have been adjusting the synaptic weight by the PSO algorithm to model the daily relations in Malaysia between precipitation and rain. In [11], the authors compare the back-propagation method versus basic PSO to adjust only the synaptic weights of an ANN for solving classification problems. In [12], the set of weights are evolved using the Differential Evolution and basic PSO.

The three main elements of the ANN have evolved simultaneously in other works such as [13]: architecture, transfer functions and synaptic weights. In [14], the authors solved the same problem using the Differential Evolution (DE) algorithm. They proposed a new PSO model. Another example is [15] in which authors develop an ANN design with two different fitness functions using an Artificial Bee Colony (ABC).

This research has significant contributions in comparison with these last three works. First and foremost, there are eight fitness functions to address three common problems arising from the ANN design: accuracy, overriding and reducing ANN. In this respect, fitness functions take classification error into account, mean square error, validation error, architecture reduction and a combination of problems that arise while designing the ANN. This research further examines the behaviour, using different parameter values, of the three bioinspired algorithms. The values of the best parameter for these algorithms will be determined to achieve the best results during the experimentation phase. Furthermore, the best configuration for each selected classification problem is used to create a set of statistically valid tests. In addition, the results obtained by the proposed methodology are presented and discussed regarding the connection number, the number of the neuron and the transfer functions selected in the ANN. Another contribution of this research is related to a new metric that allows comparing efficiently the results provided by an ANN generated with the proposed methodology. This metric takes into account the recognition rate

obtained during training and testing stages where testing accuracy is more weighted in comparison to training accuracy. Finally, the results achieved by the three bioinspired algorithms are compared against those achieved with two classic learning algorithms. The selection of these three biological - inspiring algorithms is based on the metaphor for a basic PSO technique, because NMPSO is a relatively new algorithm (in 2009). It is important to compare its performance to other algorithms that are motivated by the same.

In general, the problem to be resolved can be defined as a set of input patterns, and a set of the desired patterns, and an ANN is found represented by the function to be determined by so that the maximum number of neurons is minimized and defined. It is important to note that three fields (architecture, synaptic weight and transfer functions) form part of the search space.

This research offers a comprehensive study of how the application of bioinspired algorithms can be automated by an ANN, in particular by applying Basic Particle Swarm Optimization (PSO), Second-Generation PSO (SGPSO) and New PSO Model (NMPSO). In order to design the ANNs that are most exact in a particular problem, the proposed methodology evolves at the same time the architecture, the synaptic weights and the type of transfer functions. Moreover, a comparison of the Particle Swarm algorithm performance versus classic learning methods (back-propagation and Levenberg-Marquardt) is presented. In addition, in this research is presented a new way to select the maximum number of neurons (MNN). The accuracy of the proposed methodology is tested solving some real and synthetic pattern recognition problems. In this paper, we show the results obtained with ten classification problems of different complexities.

3. METHODOLOGY

3.1 DATA RESOURCE

Dr. William H. Wolberg's Madison University of Wisconsin Hospitals has obtained the database on breast cancer. If you publish results when using this database, please include this information in your acknowledgement. Please quote one or more of:

1. O. L. and W. Mangasar. SIAM, volume 23, No. 5 September 1990, pp1 & 18. H. Wolberg: "Cancers cancer diagnosis through linear programming"
2. H. Wolberg William and O.L. Mangasarians, Proceedings of the National Academy of Sciences, U.S.A. Volume 87, 1990, pages 9193 - 9196 (Mangazar: Multi surface pattern separation for medical diagnoses for breast cytology).
3. O. R. Setiono, and W.H. L. Mangasarian. Wolberg: "Linear programming pattern recognition: medical diagnostic theory and application" in Thomas F. Coleman and Yuying Li, publishers, Philadelphia 1990, pp 22 - 30. "Spanish diagnostics, and medical diagnostic application"
4. K. P. Fabric & O. P. L. Mangasarian: "Robust linear discrimination between two linearly inseparable sets" (Gordon & Breach Science Publishers, Optimization methods and software 1, 1992, 23 - 33).

Samples arrive regularly, as Dr. Wolberg reports his clinical cases. Therefore, the database reflects this chronological collection. Please note that the results above are based on a data set of 369, while only 367 cases are present in Group 1. This is because originally 369 instances were detected, 2 deleted.

Information of Wisconsin Breast Cancer Database are described below:

- Title: Wisconsin Breast Cancer Data
- Sources:
 - Original owners: Data was published in :
 - Dr. William H. Wolberg (physician) University of Wisconsin Hospitals
Madison, Wisconsin USA

- Donor: Olvi Mangasarian (mangasarian@cs.wisc.edu)
- Received by David W. Aha (aha@cs.jhu.edu)
- Date: 15 July 1992
- Number of Instances: 699
- Number of Attributes: 10 plus the class attribute
- For Each Attribute: (all numeric-valued)
 - ❖ attribute 1 is the class label
 - ❖ All predictive attributes are nominal, taking on integer values 0-3
- Missing Attribute Values: 16
- Class Distribution: 3 classes,
 - Benign: 458 (65.5%)
 - Malignant: 241 (34.5%)

3.2 DATA PREPROCESSING

Z-Score

In the middle of a dataset, z is the default number. Technically, however, it is a measured amount of standard differences in the population or above. A z -point is a standard distribution curve parameter, as well. The range of Z scores varies from -3 standard deviations to 3 standard deviations (to go far left with the normal distribution curve) (to the right of the normal distribution)-the mean μ is known, and if the z scoring is to be carried out, the standard population deviation is known.

Z scores are a way to use "normal" populations to compare test results. There are thousands of results and units to be achieved for the test results or surveys. These results, however, often seem insignificant. For example, it might be a good piece of information to find someone weighs 150 pounds but to search for a comprehensive basis of information if some weights are compared to the average, especially if some weights are recorded in the kilogram. You can see a z score where the average person weighs.

Z-Score formula

If you have several examples, if you want to describe the default deviation (standard error), you will use the format z - score. If you have several samples.

$$Data_{new} = \frac{Data_{old} - mean}{standard\ division} \quad (3.1)$$

3.3 ARTIFICIAL NEURAL NETWORKS

The neuron structure in the human brain inspires the Artificial Neural Network. The brain learns from experiences that go beyond the range of computers and thus adapts. This modeling also allows solutions to be less technologically developed in order to reduce human involvement.

The implementation of neural networks in computing gives us a key computational advance. Computers, like complex math and face recognition, do well. However, simple patterns are hard for computers. Computers cannot analyze, generalize and transform past patterns into future actions. The advanced neural network study allows people to understand the mechanism of thoughts, for example.

The study focusses on the' brain storage data as patterns method [17]. For individual faces to analyze and recognize, some of these patterns are very difficult. This process saves information as patterns, analyzes patterns and fixes a new computer field for problems. Training and creation of these networks is involved in the neural network to solve specific problems. We can perform different techniques such as learning, behaving, forgetting and reacting, etc. through our neural network.

"All aspects of this processor are known: The human brain is still mysterious to operate accurately. In particular, the most important element in the human brain is a certain type of cell which does not appear to regenerate as opposed to the whole body. Since the only portion of the body not slowly replaced by this type of cell, we are supposed to be able to remember, think and put past experiences into practice in all our actions. These cells are all known as neurons". The neural network as the human brain's neural network offers power through its complex components, its control mechanisms and its subsystems. Genetics programming and learning are also involved. In

electro-chemical ways, neurons transmit the information between them. Depending on the classification process used, these neurons are classified into different categories. Current systems remain incompatible with the human brain. "The most basic elements of this complex and powerful organization can only replace these artificial neural networks. Neural computing has never succeeded the developer who is trying to solve problems with the human brain. Neural computing was never substituted to human brain by the development company which attempts to solve problems. It's a new way of solving problems and machinery.

Let's see the overview of human neurons. The basic element of the neural network is neuron. The biological neurons are input and subsequently subject to various non - light operations and then produce final output. Four nerve cells are typical: dendrites, somas, axons and synapses. It accepts inputs as the task of dendrites. The input is processed by Soma. Axon-transforms the processed inputs and synapses— contacts neurons. The biological neurons in structure are not too straightforward but complex.

Biology improves the understanding of neurons. By understanding the biological brain, network designers can enhance their systems further. Neural artificial networks (ANN) are computer tools which have been widely accepted in many different disciplines to model complicated problems in the real world. ANNs could be defined as structures consisting of strongly linked adaptive elements called neurons that provide massive computations for the representation of knowledge.

"The principal features of the ANN are the ability to handle inaccurate and inadequate information, the ability to manage inaccurate information, robustness, failure and failure tolerances, fault and failure tolerance."

Artificial models possess following characteristics:

1. Nonlinearity makes it more suitable for data
2. Precise prediction for uncertain data and measurement errors due to noise insensitivity.
3. High parallelism means tolerance of hardware failure and quick processing.
4. Learn and adapt to the changing environment, allowing the system to update its internal architecture.

5. The model can be applied to unlearned data by generalization.

The main goal of ANN - based computing is to develop mathematical algorithms that enable artificial neural networks to study the processing of information and to gather human brain knowledge. Patterns based on ANN may provide virtually accurate solutions to specifically formulated problems and processes that only experimental and field observations understand. “In a number of applications from modeling, classification, design recognition and multi - variable data analysis, microbiological ANNs have been applied. The digital image processing interests are derived from two main applications: improvement for human - the reading of photo information; and processing of image information for storing, transferring and representing autonome sensor machine; and defining a two - dynamic function as the image, $f(x, y)$.

“Digital image processing is the processing of digital images via digital computers. A numerous elements with a specific position and value comprises a digital picture. They are called picture elements, elements, pixels and skins. An extensive and diversified application for digital image processing”.

3.3.1 General Properties of Artificial Neural Networks

1. Nonlinear I/O mapping

The analysis of high-dimensional data has an increasing importance due to the growth of sensor resolution and computer memory capacity. Typical examples are images, speech signals and multi-sensor data. In the analysis of these signals they are represented in their entirety or part by part in a sample space. As an example, a single data point may represent a 16x16 (sub) image. A collection of these images constitutes a cloud of points in a 256-dimensional space. In most multi-sensor data sets there is a large dependency between the sensors or between the sensor elements. This is certainly true for nearby image pixels. But also more fundamentally, it is not to be expected that any physical experiment contains hundreds of degrees of freedom that are of significant importance. Consequently, multi-dimensional data sets may be represented by lower dimensional descriptions. There are various reasons why such representations may be of interest. They may reveal the structure of the data or the problem, they may be used for relating individual data points to each

other (e.g. finding the most similar one in a database) or they may be used for retrieving missing data values.

2. Generalization ability

Their capacity to generalize is one of the major advantages of neural networks. This means that a trained network can classify data from the same class that it never saw. Developers in real-life applications usually only have a small portion of all possible neural net generation patterns. The data set should be divided into three parts to achieve the best generalization:

The training is for the training of neural networks. During training, this data set error is minimized.

The validation set is used to determine the performance of neural networks in untrained patterns. A test set to finally monitor a neural net's overall performance. In the minimum validation error, learning should be stopped. The net generalizes best at this stage. If learning is not stopped, overtrainings occur, and net performance decreases over all data, even if the error is still smaller in the training data. The network must finally be checked for the third dataset, the test set, after the completion of the learning phase. Each n training cycle, ANNS performs one validation cycle.

3. Fault-tolerance (graceful degradation)

Fault tolerance is the feature that permits the system, when certain components of it fail (or one or more inside failures), to continue to operate properly. The decline in operating quality, as opposed to an unnatural system, is proportional to the gravity to which the failure is causing a total failure if it does not. Fault tolerance is especially sought in high availability or life-critical systems. When parts of a system break up, features are known as graceful degradation.

A defect-tolerant design allows a system to operate at a lower level than to fail completely if some of the system fails. When a system fails. The term is used most often to describe computer systems designed to continue to operate more or less fully in the event of a partial

failure, with reduced output or with an increased response time. In other words, the entire system is not stopped due to hardware or software problems. A motor car is designed to continue to drive in the presence of damage caused by fatigue, corrosion, manufacturing defects or impacts, when a tire has been punctured or when structural integrity is maintained. Another example is an automotive vehicle.

The tolerance of failures can be achieved by anticipating special conditions and building a system to deal with them within the scope of an individual system, and, in general, by trying to stabilize itself so as to converge the system in a faultless state. Nevertheless some kind of reproduction is better used when the consequences of an insufficient system are catastrophic or the costs of making it reliable enough are very high. In each case, the system must be able to reverse it in safe mode, if a system failure is so catastrophic. The recovery is like a reversal, but if people are present, it can be a human action.

4. Biological analogy

Analogy is a cognitive process where information or significance is translated to a different objective or linguistic expression from one particular topic–analogy or source. A less narrowly defined inference or argument from one specific to another is in comparison to the analogy of deduction, induction and abduction where at least one premise or conclusion is general. The word analogy could also refer to the relation of the source and the goal itself, often but not necessarily similar, as in the concept of biology. The atom model of Rutherford analogized the atom with the solar system. Analogy plays a major role in problem solving, including decision-making, discussion, perception, generality, remembrance, creativeness, invention, prevision, emotions, explanation, conceptualisation and communication. The analogy was argued as "the cognitive nucleus." In particular, the analogical language includes, although not metonymous, exemplification, comparatives, metaphors, like, alligories and parable. It is not methonymous, but it does not contain the identification of places, objects or persons. As if it were, phrases like, etc. and so on, and the same term also depends on the analogous understanding of the message by the receiver. Analogy is important not only in ordinary language and common sense in the fields of science, philosophy, law and humanity. Analogy is closely linked to concepts of association, comparative approach, correspondence, mathematical and morphological

equality, homomorphism and iconicity. The concept of conceptual metaphor in the cognitive linguistics can be the same as the concept of analogy. Analogy also provides a basis for all comparative arguments and experiments whose findings are conveyed to objects not examined.

3.3.2 Structure of ANN

The neural network consists of three groups, layers and phases. The phases input, covered and output.

- The activity or input unit is the raw data that the network receives.
- The cached phase is based on the data entered and the weights of the connection between the input and the cached units.
- The phase of the output depends on the activity of the cloaks and weights between the cloaked and output units.

On the basis of the layer activity, different network types exist. A simple network type is called where the hidden units can build their own input representation. Whenever each hidden unit is active, the masses of the hidden and input units can be adjusted to allow for a hide unit to choose what it is. Other architectures such as single and multilayer are also available. In a single layer each layer is connected to the other. Overall, the network of the single layer includes only entries and outputs. The inputs are supplied by a number of weights to outputs. In several layers all units have inputs, hidden and outputs in different layers.

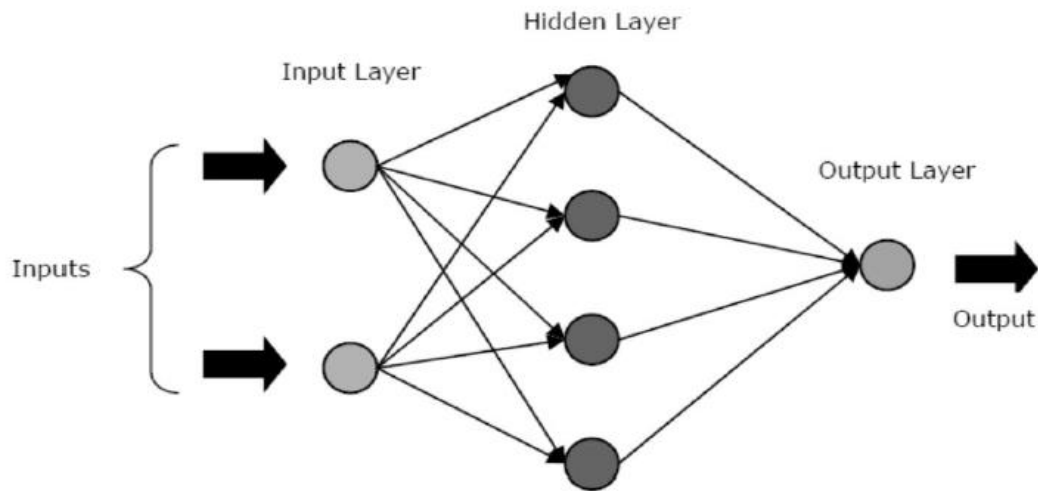


Figure 3.1: General neural network architecture

3.3.3 Elements of Artificial Neural Networks

3.3.3.1 Inputs

The data, signal, feature, or outside environment measurements are received from this layer. These inputs are generally normalized within the limits of the activation functions. The values of samples or patterns. This standardization gives greater numerical accuracy for the network's mathematical operations.

3.3.3.2 Weights

The links between neurons are assigned to the number "weights" or "parameters" in artificial neural networks. These weights change as new data are fed into the neural net. So "learns the neural net.

The weights in an artificial neural network are an estimation of the combined multiple processes in biological neurons. Myelination is important, but not important. Myelination. Weights can be positive or negative in artificial neural networks. Weight: weight is comparable to an increased combination of dendrites between neurons, numbers of synapses between dendrites, density of postsynaptic terminal neurotransmitter receptors, as well as increased formation and fusion of neurotransmitters of the vesicles and of the pre-synaptic terminals.

Positive weights: The positive weights of the synapses releasing excitation neurotransmitters (i.e. glutamate) are analogous to the pre - synaptic terminals. The receiving cell will increase its likelihood of activation.

Negative weights: Negative weights are similar to those of the neurotransmitter synapse (i.e. GABA). The receiving cell is less likely to fire a potential action.

Myelination: Myelination increases the distance between the action potential and the axon. If the axon is not myelinated, the membrane voltage potential decreases far closer to the cell body. A garden hose is analogous. If the axon does not myelinize, the garden pants are leaking, and a lower water pressure (which carries waves of water pressure, the potential action) leads to the end of the pants.

3.3.3.3 Additive Function

An additive function is an arithmetic $f(n)$ function in a positive integer that the product function is the sum of its functions when a and b are composed. $F(a) + f(b)$ holds a completely additive function even when they are not co-prime to all positive integral parts a or b if $f(b)$ holds $f(a) + f(b)$. In this sense also, analogy with fully multiplicative functions is used with complete additive. $F(1)=0$ if f is a full additive feature. Each fully additive function is an additive, but not the other way around.

3.3.3.4 Activation Function

The threshold or transfer feature is also known as activation functions. The activating functions have been used to transform neuron activation levels into output signals. Numerous activation functions are available in the neural network. Identity function, step function, part linear function and sigmoid function are various function types.

a. Identity activation function:

The activation function of identity is also referred to as "linear activation." The Network Activation function can be shown easily to fit a line regression model of the form if the ID is used in the network $Y_i = B_0 + B_1 + \dots + B_k B_k$ where $x_1, x_2, \dots, x_k$ are the k network inputs, Y_i is the i -

th network output $B_1, B_2, \dots, B_k$ are the coefficients in the regression equation. Consequently, a neural network with identity activation used in all its sensors is uncommon to be found.

b. Sigmoid activation function:

Nonlinearity in the model is used in the artificial neural network sigmoid functions. The result of a linear combination of its input signals is calculated by a network neuroelement using a sigmoid function. The sigmoid function makes an interface between the product and itself easier and more popular in the Neural Network.

$$\varphi(v) = \frac{1}{1 + \exp(-av)} \quad (3.2)$$

Sigmoid function results are generally used in learning algorithms. The Sigmoid graph is shaped as 'S'. This function is defined as an expanding function which is commonly used for neural artificial network development. Sigmoid is a function that strictly increases, and shows a balance between linear and nonlinear functions.

One - polar – is the sigmoid function.

c. Step function:

This is a unipolar threshold, known as.

$$\varphi(v) = \begin{cases} 1 & \text{if } v \geq 0 \\ 0 & \text{if } v < 0 \end{cases} \quad (3.3)$$

The neuron K output with a threshold is

$$y(k) = \begin{cases} 1 & \text{if } v_k \geq 0 \\ 0 & \text{if } v_k < 0 \end{cases} \quad (3.4)$$

v_k is the induced local field of the neuron

$$v_k = \sum_{j=1}^m W_{kj} X_j + b_k \quad (3.5)$$

When the neuron output is 1 when the local neuron field induced is not - negative, the neuron output is 0.

d. Piece Wise Linear Function

It can be defined as a unipolar function

$$\varphi(v) = \begin{cases} 1, & v \geq +1/2 \\ v, +\frac{1}{2} > v > -1/2 \\ 0, & v \leq -1/2 \end{cases} \quad (3.6)$$

When it is expected that the amplification factor is within the linear area

1. The specific circumstances of linear functions are
 - If the linear operating area is maintained without saturation, a linear combiner is produced.
 - If the linear region's amplification factor is infinitely large, it reduces to a threshold feature.

e. Learning Rules in neural network

There are many different types of study rules in the neural network, usually divided into 3 categories.

- Supervised Learning
- Unsupervised Learning

a. Supervised Learning

Training sets are available for supervised learning. This type of rule includes a set of examples with proper network behavior. The inputs are given as a training in controlled learning and the expected results are achieved. Parameters in this type of study are adjusted step by step by error signal; parameters are adjusted step by step by error signal.

A number of examples (trainings set) together with correct network conduct are provided for the learning rule.

$$\{x1, d1\}, \{x2, d2\}, \dots \dots \dots, \{xn, dn\} \quad (3.7)$$

The network input is x_n in this case and d_n is the required destination input. The output is generated by input. In order to make network outputs more exact, the Study rule is employed to change network biases and weights.

We commit ourselves with supervised learning to give the system the desired answer (d) when the entry is implemented. The distance between the real response and the desired response is used to correct the network parameter externally. For example, the error can be used to change weighing in the study of input patterns or circumstances where the answer to the error is recognised. For the learning mode, the training set, several input and output patterns are needed.

b. Unsupervised learning

In unexpected learning, self-organized learning is also known. Objective output is not available in uncontrolled learning. In that case, only network input changes weights and biases. For pattern reorganization, unattended study grouping is used. The answer required is not known in unattended learning, therefore explicit error information cannot be utilized for improving network behaviour. Information of this type is not available to correct the wrong answers so that learning has to be done based on observations of marginalized or unknown responses to the data.

The algorithms in unchecked learning use redundant row data, which have no etiquette for class membership or associations. In order to identify its parameters in this way, the network needs to detect any existing patterns, properties, regulations, etc. Unattended study means learning without the teacher because it is not necessary for the teacher to participate, but the teacher must set objectives. Feedback on neural networks is important as well. Feedback is called progressive learning, which for uncontrolled learning is very important.

3.3.3.5 Outputs

This layer contains also neurons that generate and display the final neural network outputs at the previous layers. Thus the artificial neural networks ' principal architectures can be divided, taking

into consideration the connection and the structure of the neuronal disposition. The following are possible:

- (i) Single-layer feedforward network,
- (ii) Multilayer feedforward networks,
- (iii) Recurrent networks and
- (iv) Mesh networks.

3.3.4 Classification of Artificial Neural Networks

3.3.4.1 Artificial Neural Networks According to Constructions

A. Single Layer Feed Forward Network

A neural network with a source node projecting the neural output level, but not one single feed or an acyclic network. The single layer refers to the calculation node output layer in one network layer. 3.2.

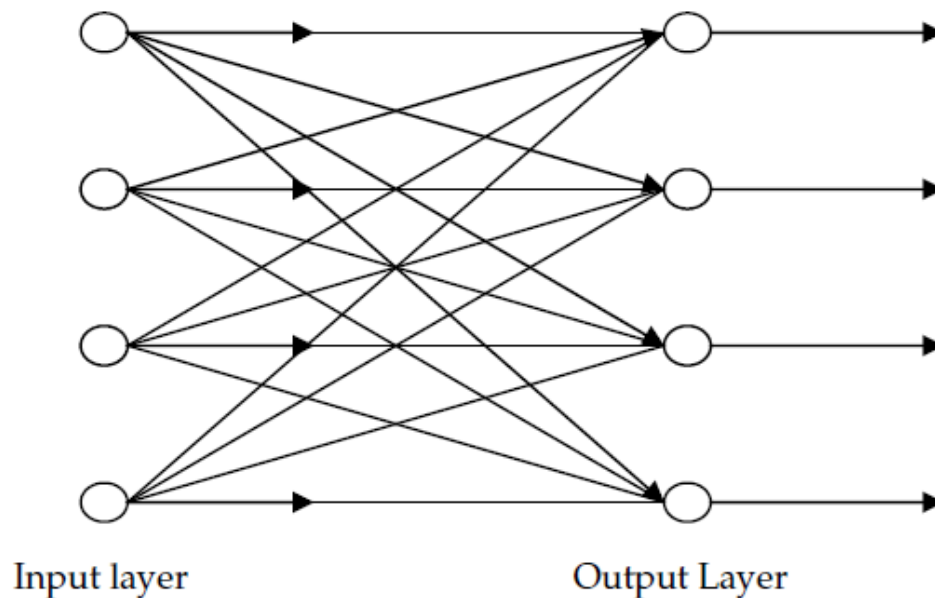


Figure 3.2: Single Layer Feed Forward Network

B. Multilayer Feed Forward Network

The system consists of at least one cache layer known as clad neurons or clad unit hubs. The ability of clad neurons is to work between external information and system output and to get separate insights on a higher demand. In the system input layer, the source hubs provide the information flag for the neurons in the second layer. The third layer of inputs are the second layer of output signals, and so on. The general reaction of the system to the actuation design provided by sources in the main layer of the info is neuron output motions in the system yield level.

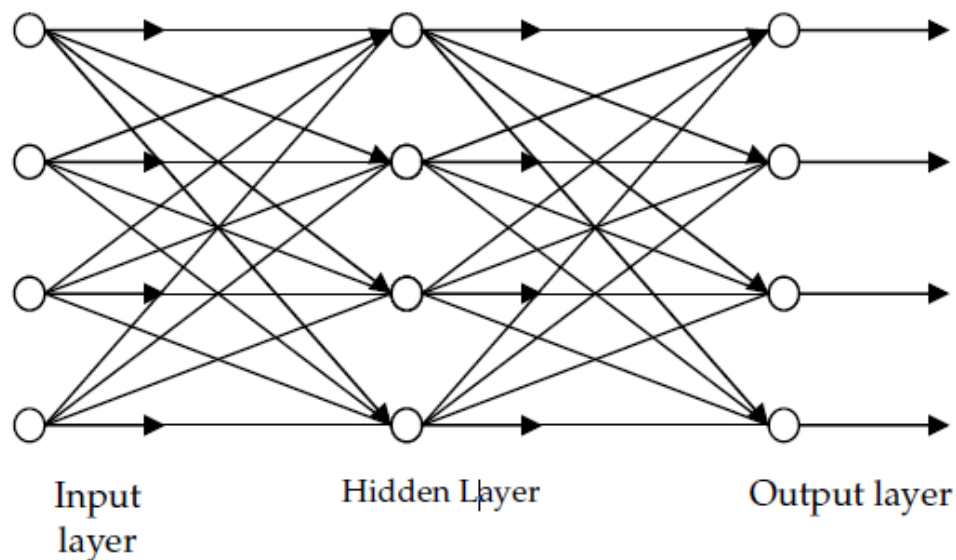


Figure 3.3: Multilayer Feed Forward Network

Short feeding network characterization:

1. In general, activation is provided via ' hidden layers ' from input to output but many other architectures exist.
2. Static input - output mappings are implemented by mathematics.
3. Most popular algorithm for backpropagation supervised training:
4. Has proved useful in many practical applications as approximations of nonlinear functions and as a classification model.

C. Recurrent Network

The repetitive system in the figure is known as a forward neural system of something like the input circle, which includes at least one shrouded layer. 2.3.2. The first time. Critics could be your own critique, i.e. if your own information returns to neuronal yield. The use of unit deferring components, which leads to a unique conduct, has sometimes been criticised, since the neural system has non-direct units.

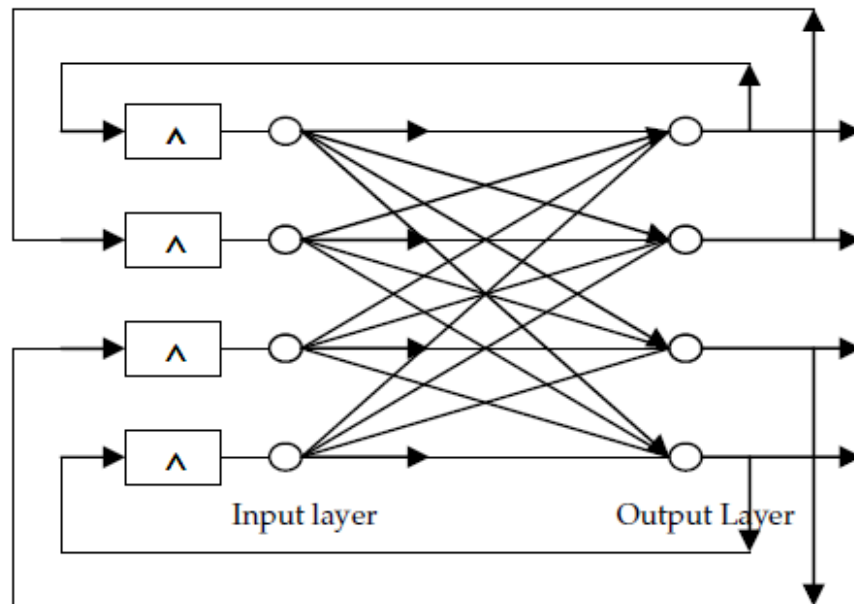


Figure 3.4: Recurrent Network

Other network types are available ; Delta - bar - delta, hop field, quantifying vectors, counterpropagation, probabilist, hamming, memory boltzman, spatium - temporal patent, adaptive resonance, auto - order, recirculation etc.

The cyclic path of synaptic connections is a recurring neural network.. Basic characteristics:

1. Recurring are all biological neural networks
2. They implement dynamic systems mathematically
3. Various types of algorithms, no clear winner, are known
4. In general, theoretical and practical problems have prevented practical applications up to now.

3.3.4.2 Artificial Neural Networks According to Learning Algorithms

If a network is structured for a particular application, it will be ready for formation. At start and beginning of training, initial weights are selected randomly. Two approaches are available; controlled and unattended.

A. Supervised Training

The inputs and outputs are provided for supervised training. The data is processed by the network and the results are compared with the results. The system spreads errors to adjust network weights. This process takes place time and again when weight is constantly changed. The same data set is processed many times during networking training, as the weight of connections is always improved. The data set for the training is referred to as the "training set."

Sometimes a network can never learn. This can take place as there are no specific information in the input data to produce the required output. Networks also do not converge when there are not enough data to enable complete learning. In order to retain part of the data as a test, there should ideally be sufficient data. Multiple nodes in many layered networks can store data. To monitor the network, the supervised training must retain data for the system to test after training of a system, to determine whether the system simply saves its data.

Then, if a network cannot simply solve the problem, the designer must examine inputs and outputs, number of layers, numeric elements per layer, layer connections, transfer and training capabilities and also initial weights. The training rules govern another part of the creativity of the designer. Many laws (algorithms) are used in the training session to make the required weight adjustment feedback. The most common method is back-propagation. It is a conscious analysis and not only a technique to prevent overtraining of the network. General statistical trends in the data are the initial setup of the artificial neural network. It then 'learns' about other aspects of the data which are generally falsified.

The weights can be frozen upon request, if finally the system is properly trained and no further training is necessary. This network can then be converted on certain systems into hardware. During production, other systems do not lock in, but continue learning.

B. Unsupervised or Adaptive Training

Uncontrolled (learning) is the other kind of training. The network has inputs but not desired outputs in this kind of way. The system must then determine its own functions in order to group the input data. Often this is termed autonomy or adaptation. These networks do not adjust their weight using external influences. Their performance is instead monitored internally. The networks seek the regularity or trends of the input signal and adjust it to the network functions. Although the network still needs to be able to provide information on how to organize itself without knowing whether or not this is right. These data are incorporated into the network's topology and study rules. The cooperation between the processing element clusters may be emphasized by an unchecked learning algorithm. The clusters would work together under such a scheme. If any external input activated a node within the cluster, it could increase the whole activity of the cluster. Furthermore, it can inhibit the whole cluster if external input to the cluster nodes has been decreased. Competition between processing elements could also provide a learning basis. Competitive cluster training could enhance the response of particular groups to special incentives. In that sense, these groups would be linked and a special appropriate response would be provided. The weight of the winning processing element is normally only updated when the learning contest is effective. Unattended learning is not well understood at the present time and a lot of research is in progress.

C. LEARNING LAWS (ALGORITHMS)

There are many common uses for learning laws. The majority are a variation of ' Hebb's rule ' which is the best - known and oldest.

Hebb's Rule: In the Compatibility Organization, Donald Hebb introduced this. The fundamental rule of thumb is that the weight should be strengthened if the neuron comes from another nerve and both neurons are very active (the same sign).

Hopfield Law: Increase connectivity weight by the study rate and when both active and inactive the desired outcomes and inputs.

The Delta Rule: The idea is that the strengths of the input connections can constantly be modified so that the difference of the desired output to the actual output of the element is reduced (delta).

The Gradient Descent Rule: This is similar to the Delta rule because the transfer function derivative is still used to change the delta bug prior to the application of connection weights. However, a proportional additional constant associated with the learning rate accompanies the final weight - based change factor.

Kohonen's Law: This allows processing parts to acquire or update their weight. The strongest item is declared the winner and its competitors can be inhibited and its neighbours excited. Only the winner can adjust his weight and only the winner plus neighbors can adjust it.

3.3.5 Artificial Neural Network's Output Calculations

Sensitivity, septicity and accuracy are preferred statistics for determining the performance of a classifier. Susceptibility is the estimation rate for patients with epileptic diseases, speciality is the estimation speed for healthy people and accuracy is true. Equality. These statistical numbers are calculated using (36), (37) and (38).

$$Sensitivity = \frac{TP}{TP+FN} \quad (3.8)$$

$$Specificity = \frac{TN}{TN+FP} \quad (3.9)$$

$$Accuracy = \frac{TP+TN}{TP+FP+TN+FN} \quad (3.10)$$

In the above equations, the number of TP - diagnosed epileptic patients, the total number of normal epileptic patients, for whose epileptic disease was diagnosed, and the total number of normal epileptic patients, for which FN was diagnosed.

3.4 GENETIC ALGORITHM

The genetic algorithm biological metaphor is the evolution of species by the survival of the fittest, as Charles Darwin described. A new individual is produced by the crossover of genetic information of two parents in a population of animals or plants. The DNA stores the genetic data for the individual's construction. The genome of human DNA comprises 46 chromosome, four strings, abbreviated A, T, G and C. One of twenty amino acids, or a 'start protein building' or 'stop protein building' signal, is translated into three bases. A total of about 3 billion nucleotides are present. These can be structured into genes that contain information about the individual's construction in one or more parts. The vast majority of genes –the "junk" genes –are not being used, however, and only 3% of all genes contain meaningful information. Genetic data, the genome itself, are called the individual's genotype. The result is called a phenotype. The individual. The same genotype could lead to various phenotypes. This is clearly illustrated by the Twins. The process of natural evolution is simulated by a genetic algorithm. It aims at optimizing a number of parameters. The original idea includes the genetic information, called a parameter string, or an individual, in a bit string of a fixed length. An allele is called a possible value of a bit. A range of different encoding techniques are used in this thesis, but the fundamental principles also apply. A possible solution to this problem is provided by each parameter string. It includes information about building a neural network for the GANN issue. The fitness value is the quality of the solution. Crossover, selection and mutation are the fundamental GA operators. The main structure of a genetic algorithm is shown in Figure 1. It begins with the random generation of an early group of people, the original population.

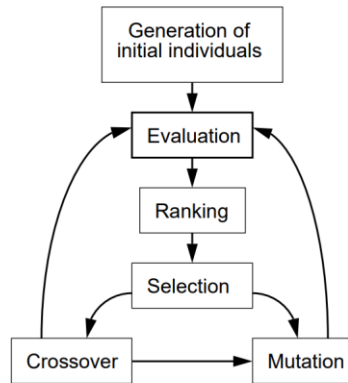


Figure 3.5: The Principle Structure of a Genetic Algorithm

Evaluate and classify individuals. Since the number of persons is constant in each population, an old person, generally the one with the worst fitness value, must be discarded for each new individual. Two basic operators are available to create new people: mutation and intersection. Mutation is simpler. A few bits of the parameter string are rotated at random during mutation. Mutation may apply to offspring created by crossover or randomly to any person in the population as an independent operator.

1. Crossover

Crossover simulates a child's or two parents' sexual generation. This is done by taking parts of one parent's bit string and the other parent and combining both parts of the child. The crossover consists of three main types: one, two and uniform. Figure 1.4 shows one-point crossover. At the same point, the two parent bit strings are cut. So one part of each parent can generate the child. Notice not moving the parts. The random cutting point is also independent of the true significance of the bits. One bit string parameter can be encoded in more than one bit, with the encoding cut to a new value, different than the two parents, during the crossover.

2. Selection

The choice of people for crossover and mutation is prejudicial to good people. The chance of a selected person is based on the relative fitness of the classical roulette wheel population.

3. Mutation

In real evolution, by misrepresentation or other gene deformations e.g. gamma radiation, the genetic material can randomly modify itself. Mutations can be performed with a certain probability in genetic algorithms as random deformations of the strings. It is positive that genetic diversity is maintained and the local maxima avoided.

4. Sampling

From the first and the next generation, this process calculates. We can indicate the following substantial differences in comparison with conventional continuous optimization methods, such as Newton or the descent gradient:

1. GA manipulates coded versions of the problem parameters, i.e. search room S instead of X itself instead of parameters themselves.
2. While looking for nearly all conventional methods, GAs are always working on a whole population of items (cords). The force of genetic algorithms is greatly enhanced. The chance to reach the best level in the world has been improved and the risk of being caught in a fixed region is reduced vice versa.
3. No additional information about objective value of function like derivatives is used by normal genetic algorithms. It can therefore be used in the event of continuous or discrete optimization problems. Only a valuable decoding function should be specified.
4. Deterministic transitional operators are applied by GAs while conventional continuous optimisation methods. In particular, there are some random components of how a new generation is determined from the current one (examples are shown later).

3.4.1 Binary Strings Genetic Operations

3.4.1.1 Selection

The solution algorithm is chosen by preferred fitness people rather than fitness fitness people. It may be a decisive task, but it has random components in most implementations. The following version is very popular now, where the chances of selecting a certain person are proportional to their health, (We will give a theory explaining the good properties later). A random function experiment can be considered:

$$P[b_{j,t} \text{ is selected}] = \frac{f(b_{j,t})}{\sum_{k=1}^m f(b_{k,t})} \quad (3.11)$$

Of course, only when all fitness values are good is this formula meaningful. Unless this is the case, in the simplest case the transformation $5 - 0 \cdot$ does not decrease. (In the simplest case the shift should be applied). The likelihood can be expressed

$$P[b_{j,t} \text{ is selected}] = \frac{\varphi(f(b_{j,t}))}{\sum_{k=1}^m \varphi(f(b_{k,t}))} \quad (3.12)$$

By random test, a generalized Roulette Game, to some degree we can force the property (2.1) to be met. The slots are not as wide in this roulette game, i.e. the various results can take place with different probabilities. The graphic indication of how this wheel game works is provided by Figure 2.1.

3.4.1.2 Crossover

When parents mix up their gametes, the genetic materials of both parents are mixed as they appear in the real world. As a result, certain genes are generated by one parent and the other parents. Chromosomes are generally divided and combined randomly.

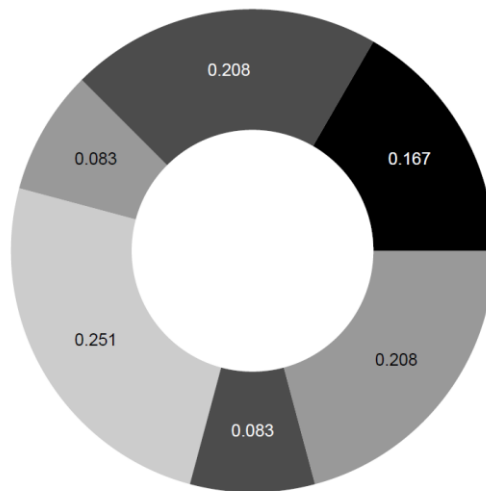


Figure 3.6: A graphic representation of selection of roulette wheels with 6 alternatives m . The numbers within the arcs correspond to the likelihood of selecting the alternative.

This is known as the crossover mechanism. It is an excellent tool for the introduction of new genetic resources and for preserving genetic diversity, but also for providing better children or good parents. Several studies have found that crossover is why species sexually adapted to reproduce faster than those that asexually replicate. Crossover is primarily gene exchange for both parents' chromosomes. You can achieve this by randomly selecting two strings and in the simplest case, changing the two tails. In figure 2.2 this process is called a crossover with one point below.

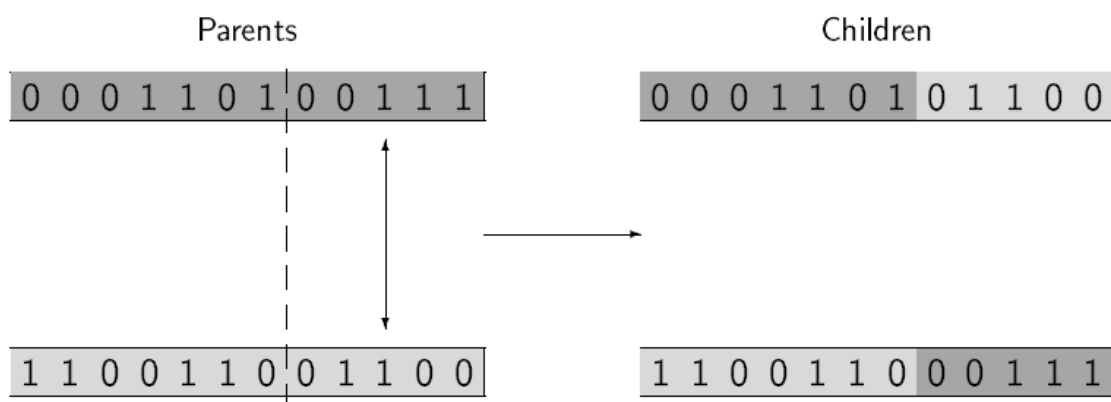


Figure 3.7: One-point crossover of binary strings

One - point crossover for Gas that operates on binary strings is a simple and common method. Additional methods of crossover can be useful or even necessary for other problems or different coding.

N-point crossover: N breaking points are randomly selected instead of just one. Each section is exchanged. Two crossover points are especially important for this class.

Segmented crossover: This is similar to N - point crossroads, as the breaking points differ.

Uniform crossover: It is randomly decided whether the positions are exchanged for each position.

Shuffle crossover: The first two parents receive a randomly selected permutation, then the shuffled parents receive the N point cross, and then the shuffled kids return the other way round.

3.4.2 Mutation

Mutation — a random deformation of an individual's genetic data by radioactivity or other environmental influences is the ultimate part of our genetic algorithm. The probability of a mutation of a certain gene for all genes is nearly equal. In real reproduction P_m should of course be quite low to prevent the GA from acting like random searches chaotically. Again, it is coding and the problem itself that are the choice of the correct mutation method, similar to a crossover.

Single bit reversal: One bit is randomly rejected with probability P_m .

Bitwise inversion: The entire string with prob p_m is gradually inverted.

Random selection: The string is replaced by an altered selected one with the probability P_m .

3.4.3 Examples

3.4.3.1 Simple Example

Take into account the problem of finding the maximum global function:

$$f_1: \{0, \dots, 31\} \rightarrow R$$
$$x \rightarrow x^2 \tag{3.13}$$

Of course, it is obvious but it is possible to calculate some steps alone in order to obtain insight into genetic algorithms by the simplicity of this problem.

Of courses, a good string space along with the relevant coding and decryption scheme will naturally be the first step in the checklist. In order to do GA work, this is necessary. In this example, $S \succ \{0, 1\}^5$, where a value of $\{0\}$ is close to hand, can be considered. The binary representation of 31 is coded. A string is decoded as a consequence

$$c(s) = \sum_{i=0}^4 s[4-i] \cdot 2^i \quad (3.14)$$

Assume that with a population size of $m = 4$ we have Algorithm 2, 5 as it is with a crossover likelihood of $P_c = 1$ and P_m mutation likelihood = 0,001. When we randomly calculate the first generation with a consistent distribution over $\{0, 1\}^5$, in the first step we obtain the following:

Individual No.	String (genotype)	x value (phenotype)	$f(x) = x^2$	$P_{select_i} \frac{f_i}{\sum f_i}$
1	0 1 1 0 1	13	169	0.14
2	1 1 0 0 0	24	576	0.49
3	0 1 0 0 0	8	64	0.06
4	1 0 0 1 1	19	361	0.31

The fitness value is 1170, where the average is 293 and the maximum is 576. It can easily be calculated. The last column shows that proportional selecting favors people with high fitness conditions (as No. 2) compared to those with low fitness (as No. 3).

Set of selected individuals	Crossover site (random)	New population	X value	F(x) X^2
0 1 1 0 1	4	0 1 1 0 0	12	144
1 1 0 0 0	4	1 1 0 0 1	25	625
1 1 0 0 0	2	1 1 0 1 1	27	729
1 0 0 1 1	2	1 0 0 0 0	16	256

Thus we obtain an average of 439 and a maximum of 729 fitness values from the new generation of 1754. This very basic example shows how selection favors qualified people and how cross-over between two parents can create a baby even better than the two parents. The reader is left to follow this example as an exercise.

3.4.3.2 A One - Dimensional Oscillating Feature

Now we want to know how much the function can achieve globally

$$f_2 : [-1, 1] \rightarrow R \quad (3.15)$$

$$x \rightarrow 1 + e^{-x^2} \cdot \cos(36x) \quad (3.16)$$

The function can be seen from the plots in Figure 2.3 and has a global maximum of 0 and numerous local maximums. Firstly, the search space $[-1, 1]$ must be discretized in order to work with binary strings. A uniform grid of $2n$ points is common practice and grid points are listed then and the binary representation of the index is employed as a codification.

The algorithm reaches the global high point after 52 generations, with an average of $52 \times 6 = 312$ fitness evaluations, and the search area's total size is $216 = 65536$. At least in this example, we can conclude that the GA is definitely better than the random search or the comprehensive method which scans the entire search area dumbly. Take 0111111111111111 to find out more about the

coding / decoding scheme. The number of the integer is 32767. Decoding function rates are computed

$$-1 + 32767 \cdot \frac{1-(-1)}{65535} = -1 + 0.9999847 = -0.0000153 \quad (3.17)$$

3.4.3.3 A Two-Dimensional Function

In this example we find that the GA definitely is much faster than a big or random algorithm for research. The problem comes with a smooth f3, which results can be achieved using a standard method by changing the initial values. The maximum global (0, 0) is obviously circled by the minimum ring and in this example has a radius of $\pi/2$. The global maximum is likely to converge when this is an original value, but only for example when BFGS is used (Broyden Fletcher Goldfarb Shanno, an efficient Quasy - Newton method for continuous uncontrolled optimization of functions [10]). The chance of the corresponding neighborhood value is the maximum when the initial value is assumed randomly by $[-10, 10]$.

$$\frac{\left(\frac{\pi}{2}\right)^2 \cdot \pi}{10 \cdot 10} = \frac{\pi^3}{400} = 0.0775 \quad (3.18)$$

Consequently, until an initial value is reached, the expected test number is $1/0.0775/13$. The BFGS method with line search required the right global optimum during test implementation of the BFGS method for 15 tests (random initial values). For these computations, the total time for SGI O2 (MIPS R5000/180SC) was 5 milliseconds. As mentioned above, it took 1.5 seconds for the genetic algorithm to be compared to the global optimum.

This example demonstrates that GAs are not necessarily quick. In addition, in many cases the methods involved in derivatives are much slower than conventional ones. The next example, however, dramatically demonstrates that even fluid functions in conventional optimization techniques are difficult to implement.

3.4.4 Genetic Programming

In their daily practice, mathematicians and computer scientists only search for programs that correctly solve the problems. You usually attempt to design such programs based on your knowledge, underlying principles, mathematical models, intuition and so on. The questions of Koza look somehow utopian and provocative. However, his answers are remarkable and worthy of further discussion here. The basic idea is simple but appealing—the problem of automatic program induction should involve genetic algorithms. All we need to do is change all the genetic techniques that we have talked about so far. Random initiation, connection and mutation are involved. We need nothing new to choose and sample, because these processes are independent from the display of the data.

Of course, that sounds great. However, the question arises as to whether this type of genetic programming (GP) is working. Koza starts with a rather vague hypothesis in his remarkable monograph [30].

The Paradigm of genetic programming: Provided that we have a resolvable problem, a definition for a suitable programme, a sufficient number of representative test examples, WWa genetic algorithm can determine which (approximately) program solves the problem and provides us with sufficient representative test examples. It appears to be a question of faith. This hypothesis has not been demonstrated by anyone so far and it is doubtful whether this is ever possible. Rather than providing evidence, Koza has developed many well - chosen examples which empirically highlight his hypothesis. The successful solutions with GP include:

- Control of the process (inverted pendulum bang bang control)
- Logistics (simple robotic control, problems with stacking)
- Automatic scheduling (pseudo - random number generators, ANN design)
- Game strategies (Poker, Tic Tac Toe)
- Inverse kinematics
- Classification

- Symbolic computation:
 - Sequence induction (Fibonacci sequence, etc.)
 - Symbolic regression
 - Solve equations (functional, differential and integral equation power series - based solutions)
 - Symbolic differences and integrity
 - Trigonometric identity discovery automatically

A brief introduction to genetic programming has been given in this chapter. We will focus on the basic methodological problems and will omit detailed examples.

3.5 TRAINING OF ARTIFICIAL NEURAL NETWORKS

The neural biological computing systems that make up animal brains are artificial neural networks or connecting systems. Such systems learn tasks by following examples, usually without task-specific programming (a step towards improvements in performance). You can learn how to identify images that contain the Cats and use the results to identify the Cats in the other images through the analysis of flames that manually mark "cat" or "no-cat." They don't know cats, for example, fur, tails, whiskers and cat - like faces. Rather, from the learning material they are processing they develop their own set of relevant features. An ANN is based on an artificial neuronal collection which is linked with the unit or node (analogous to biological neurons in the animal brain). Any link between artificial neurons (similar to a synapse) can signal them. The artificial neuron receiving the signal can proceed and signal the connected artificial neurons.

In the common ANN implementation, the signal is an actual value in the relation between artificial neurons, and the output is calculated by a nonlinear input sum function from each artificial neuron. Artificial neurons and connections usually weigh in accordance with learning. The weight increases or lowers the signal strength of the connection. An artificial neuron threshold can only be present if the aggregate signal crosses this threshold. Artificial neurons are usually arranged in

layers. Inputs can be converted into different types by different layers. Signals travel from the first layer to the last layer (output), maybe several times after the layers have been passed through.

The original objective of the ANN approach was to solve problems like the human brain. The focus was over time on matching specific mental skills that lead to biodiversity. Different tasks such as computer vision, speech recognition, machine translation, social network filtering, video games and playboards and medical diagnosis are performed using ANNs. This section shows a training process that optimizes ANN performance through BP and GA algorithms.

3.5.1 Training Artificial Neural Networks with Backpropagation.

The method of gradient descent includes the derivatives of the squared error function with respect to the weight of the network. This is usually done in return. The squared error function takes the following:

$$E = \frac{1}{2}(t - y)^2 \quad (3.19)$$

where

E is the error squared,

t is the target output for a sample training, and

y is the current output of neuron output.

The $1/2$ factor in the exponent is distinguished. Then the term is increased by an arbitrary learning rate. Whether a continuous coefficient is implemented now is not important.

For each neuron j , its output o_j is defined as

$$o_j = \varphi(net_j) = \varphi(\sum_{k=1}^n w_{kj} o_k) \quad (3.20)$$

The netj input for the neuron is the weighted sum of previous neuron outputs. The ok of the input layer is simply a xk input in the network. If the neuron is in the first layer after the input layer. The input units in the neuron are numbered by n. The wkj variable shows the weight from the neuronal to the j.

β is non - linear and distinctive with the activation funktion. The logistic function is a commonly used activation feature:

$$\varphi(z) = \frac{1}{1+e^{-z}} \quad (3.21)$$

which has a convenient derivative of:

$$\frac{d\varphi}{da} = \varphi(a)(1 - \varphi(a)) \quad (3.22)$$

Identifying the error derivative

Twice by the chain rule is calculated the partial derivation of an error in relation to a wij:

$$\frac{\partial E}{\partial w_{ij}} = \frac{\partial E}{\partial o_j} \frac{\partial o_j}{\partial net_j} \frac{\partial net_j}{\partial w_{ij}} \quad (3.23)$$

In the last right side factor of the foregoing w_{ix} depends only one term in the sum net_h

$$\frac{\partial E}{\partial net_j} = \frac{\partial}{\partial w_{ij}} \varphi(\sum_{k=1}^n w_{kj} o_k) = \frac{\partial}{\partial w_{ij}} w_{ij} o_i = o_i \quad (3.24)$$

When the first layer of the neuron after the input layer is, o_i is only X_i .

With respect to the input, only the active function parameters are a derivative of neuron j output (if logistics function is used):

$$\frac{\partial o_j}{\partial net_j} = \frac{\partial}{\partial net_j} \varphi(net_j) = \varphi(net_j)(1 - \varphi(net_j)) \quad (3.25)$$

That is why a differentiated activation function is required for back propagation. (The activation function of ReLU, which cannot be differentiated by 0, is very popular in the recent past, for instance in AlexNet)

The first factor to evaluate is simple, because then $o_j = y$ and if the neuron is in the output layer.

$$\frac{\partial E}{\partial o_j} = \frac{\partial E}{\partial y} = \frac{\partial}{\partial y} \frac{1}{2} (t - y)^2 = y - t \quad (3.26)$$

But if j is within an arbitrary inner network layer, it is less obvious to determine derivative E with respect to the o_j .

$$\frac{\partial E(o_j)}{\partial o_j} = \frac{\partial E(net_1, net_2 \dots net_u)}{\partial o_j} \quad (3.27)$$

Taking into account E as a function where all neurons are inputs ($L=1, 2 \dots u$)

$$\frac{\partial E}{\partial o_j} = \sum_{\partial \in L} \frac{\partial E}{\partial net_j} \frac{\partial net_j}{\partial o_j} = \sum_{\partial \in L} \frac{\partial E}{\partial o_j} \frac{\partial o_j}{\partial net_j} w_{j\partial} \quad (3.28)$$

Thus, if all derivatives are known with respect to o_j — that which is closer to the neuron output — the derivative with regards to o_j can be calculated. Combining everything:

$$\frac{\partial E}{\partial w_{ij}} = \partial_j o_i \quad (3.29)$$

In 1960 Henry J. Kelley and 1961 Arthur E. Bryson derived the basics of continuous back-propagation from control theory. They have used dynamic programming principles. A simple derivation based only on the chain rule was published in 1962 by Stuart Dreyfus. This is a multi - phase method used to optimize dynamic systems by Bryson and Ho in 1969.

In the beginning of the 1960's, background propagation was derived by a number of researchers and launched by Seppo Linnainmaa as early as 1970, for instance Arthur E. Bryson and Yu-Chi Ho, among the researchers of the 1960s. After a careful analysis in his PhD dissertation in 1974, the first person to propose use for neural networks in the United States was Paul Werbos. The prize for work of David E. Rumelhart was awarded in 1986 to Geoffen E. Hinton, Ronald J. Williams & James McClelland.

The general automated differentiation (AD) method of discernible connected networks for nestled differentiating functions was issued by Linnainmaa in 1970. This is the backbone that even with sparsely networked networks is efficient. Backpropagation was used in 1973 by Dreyfus to adapt

controller parameters in proportion with error gradients. Werbos noted the potential to apply this principle to neural artificial networks in 1974, and in its current application on neural networks employed the Linnainmaa AD Method in 1982.

In 1986, Rumelhart, Hinton and Williams proved that the process could produce useful internal images of inbound data in hidden layers in neural networks. Wan was the first winner in 1993 of an international competition for pattern recognition. In the 2000s it was disadvantageous, but it came back in 2010 with cheap, high-performance computer systems based on GPUs. In particular, research was conducted into linguistic structures, where connectivity models could explain a number of first language and second language learning phenomes using this algorithm.

4. IMPLEMENTATION AND RESULTS

Comparative Results

Dataset Preprocessing

The dataset had some missing values which was fix using SPSS's Estimation-Maximization (EM) algorithm and then processed using z-score for artificial neural network training.

Expectation-maximization algorithm

An EM - algorithm is an iterative method in statistics in which a model is based on unconsidered latent variables to identify the most likely or maximum posterior estimate (MAP). In order to determine the distribution of variables in latent variables in step E, EM iteration changes the performance of E-step, creating a programmable expectation function evaluated by the existing parameter estimate and a M-step, calculating the parameters that maximize the expected log likelihood at Step E.

Z-Score

Simply put, z is the default number of the average dataset. However, the standard differentiation below or above population is more technically measured. Also a z-point can be placed in the normal distribution curve as the default score. Z-scoring varies from -3 default deviations to + 3 standard deviations (where the distribution curves take the right side) to + 3 standard deviations (the far-left one). You have to know the medium μ and standard population differences if you want z-score to be used.

Z values are a way of using "normal" populations to compare test results. There are thousands of results and units to be reached in test results or surveys. However, these results often appear insignificant. For instance, it could be good information to know that someone is 150 pound weight, but to look at an extensive database, especially if some weights are recorded in kilograms, if you want to compare it with the "average." A z - score can indicate where the person's weight is compared to the average population weight.

Breast Cancer Results

First we present the individual for ANN-GA using Breast Cancer dataset. We used 20 neurons the hidden layer. Figure 1 and 2 are showing the fitness or Root Mean Squared Error (RMSE) or error outcomes by using the existing ANN-GA approach for 2000 iterations.

Figure 1 contains the error calculation process for 2000 iterations for artificial neural network training with 20 neurons in the hidden layer. Figure 2 contains the prediction and the classification of artificial neural network compared with the targets attribute in the dataset.

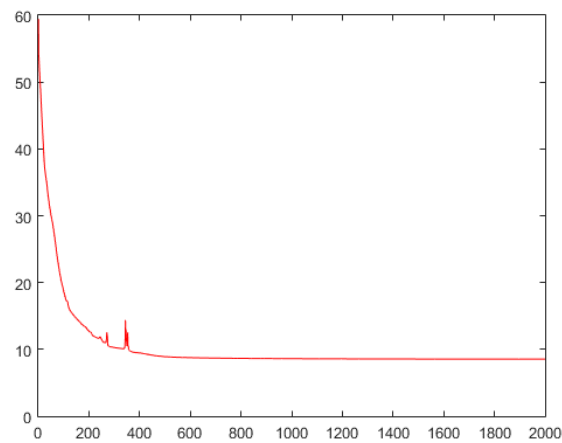


Figure 4.1: Error graph performance using ANN-GA for Breast Cancer Dataset

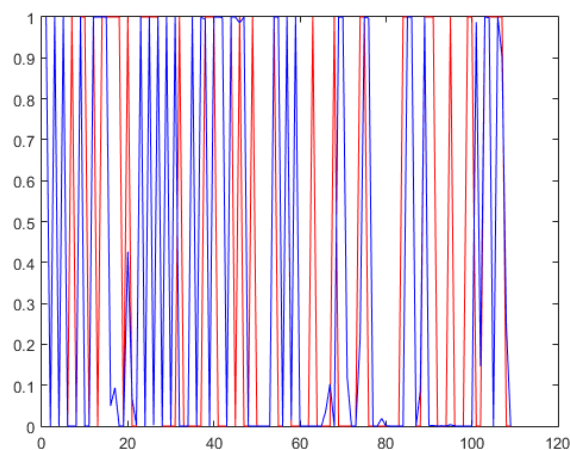


Figure 4.2: Error iteration graph performance using ANN-GA for Breast Cancer Dataset for original target and predicted outcomes.

Table 4.1: The collected results

Training Error (Fitness/RMSE)	0.0463
Training Accuracy	95.37%
Testing `Error(Fitness/RMSE)	0.06926
Testing Accuracy	93.074%
Training Sensitivity	0.980079
Training Specificity	0.939674
Testing Sensitivity	0.957832
Testing Specificity	0.910392

Table 4.1 contains the results for the method according to Figure 4.1 and Figure 4.2 which show the training error and accuracy, testing error and accuracy (using RMSE as a fitness function) and both the specificity and sensitivity for training and testing.

5. CONCLUSION

The comparative results showing that using the advantages novel GA algorithm we can able to optimize the performance of ANN training and testing to solve the real time problems. From these experiments, we observed that the fitness functions that generated the ANN with the best weighted recognition rate were those that used the classification error. The GA was compared in terms of the accuracy, error rate, sensitivity rate, specificity rate and accuracy rate for both training and testing perspective with other researchers. The GA algorithm achieved the greate performance. The transfer functions that more often were selected for each algorithm were: the Gaussian functions for the basic BP algorithm; the sinusoidal function for GA algorithm. In general, the ANNs designed with the proposed methodology were very promising. The proposed methodology automatically designs the ANN based on determining the set connections, the number of neurons in hidden layers, the adjustment of the synaptic weights, the selection of bias, and transfer function for each neuron.

5.1 SUGGESTIONS

In this research work, we perform the ANN training using GA algorithm using the research datasets. For future suggestions we want to perform below points:

- The current evaluation is based on single class problems for classification, however under the real time scenario this will not be the case always. So we suggest evaluating the performance of proposed model using multi-class datasets.

Second point is, the consideration of more real time will be the interesting future direction for this research work.

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